

## Math, 7

*Communicates clearly and explains reasoning so others can follow how a problem is solved.*

: Uses appropriate mathematical language.

: Uses appropriate forms of mathematical representations to present information correctly.

: Moves between different forms of mathematical representations.

: Communicates through lines of reasoning that are complete and coherent.

### ALT 6 - Communication Rubric

<p style="text-align: center;"><b>4</b></p> <p style="text-align: center;"><b>Highly Proficient</b></p>	<p style="text-align: center;"><b>3</b></p> <p style="text-align: center;"><b>Proficient</b></p>	<p style="text-align: center;"><b>2</b></p> <p style="text-align: center;"><b>Nearly Proficient</b></p>	<p style="text-align: center;"><b>1</b></p> <p style="text-align: center;"><b>Developing</b></p>
<ul style="list-style-type: none"> <li>• The pathway to a solution is precise, elegant, and clearly leads to an identified solution.</li> <li>• The explanation connecting each of the parts is given using precise mathematical language.</li> <li>• The mathematical writing is elegant, precise, and there are no errors in concepts or connections.</li> </ul>	<ul style="list-style-type: none"> <li>• Show my work such that the pathway to the solution is clear.</li> <li>• Correctly use math words and symbols in my work and final solution.</li> <li>• Express my final answer clearly and in context for contextual problems.</li> <li>• Express my understanding of the connections and concepts of mathematics in writing.</li> <li>• Use correct units when expressing my conclusion.</li> </ul>	<p>One or more of the following are occurring in the work...</p> <ul style="list-style-type: none"> <li>• The pathway to the solution is not clear.</li> <li>• The path to the solution leaves out important parts of the work.</li> <li>• The math words and/or symbols used are not always correct.</li> <li>• The final answer is not clearly evident.</li> <li>• The final answer is not in context for a contextual problem and/or does not have the correct units for the problem.</li> <li>• Some mathematical connections or concepts expressed correctly in writing.</li> <li>• The path to complete the work is just started.</li> </ul> <p style="text-align: center;">OR</p> <ul style="list-style-type: none"> <li>• The parts of the solution do not connect to each other.</li> </ul>	

		<p>OR</p> <ul style="list-style-type: none"> <li>No steps are shown, only a final answer is given.</li> </ul> <p>OR</p> <ul style="list-style-type: none"> <li>Mathematical writing unclear or incorrect.</li> </ul>
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*Reasons mathematically to solve problems in real-life context.*

: Identifies the relevant elements of the authentic real-life situation.

: Selects adequate mathematical strategies to model the authentic real-life situation.

: Applies the selected mathematical strategies to reach a valid solution to the authentic real-life situation.

: Explains the degree of accuracy of the solution.

: Explains whether the solution makes sense in the context of the authentic real-life situation.

**ALT 2 - Modeling Rubric**

<b>4</b> Highly Proficient	<b>3</b> Proficient	<b>2</b> Nearly Proficient	<b>1</b> Developing
<p>The student is able to:</p> <ul style="list-style-type: none"> <li>identify the relevant elements of the authentic real-life situation</li> <li>select appropriate mathematical strategies to model the authentic real-life situation</li> <li>apply the selected mathematical strategies to reach a correct</li> </ul>	<p>The student is able to:</p> <ul style="list-style-type: none"> <li>identify the relevant elements of the authentic real-life situation</li> <li>select adequate mathematical strategies to model the authentic real-life situation</li> <li>apply the selected mathematical strategies to reach a valid</li> </ul>	<p>The student is able to:</p> <ul style="list-style-type: none"> <li>identify the relevant elements of the authentic real-life situation</li> <li>select, with some success, adequate mathematical strategies to model the authentic real-life situation</li> <li>apply mathematical strategies to reach a solution to the authentic real-life situation</li> <li>discuss whether the solution makes sense in the context of</li> </ul>	

<p>solution to the authentic real-life situation</p> <ul style="list-style-type: none"> <li>justify the degree of accuracy of the solution</li> <li>justify whether the solution makes sense in the context of the authentic real-life situation.</li> </ul>	<p>solution to the authentic real-life situation</p> <ul style="list-style-type: none"> <li>explain the degree of accuracy of the solution</li> <li>explain whether the solution makes sense in the context of the authentic real-life situation.</li> </ul>	<p>the authentic real-life situation.</p>
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*Recognizes patterns and describes them as relationships or general rules.*

: Selects and applies mathematical problem-solving techniques to correctly identify the pattern.

: Pattern is described as relationship or general rule.

: Verifies the validity of these general rules.

: Conclusions are consistent with the correct findings.

**ALT 3 - Patterns Rubric**

<b>4</b> <b>Highly Proficient</b>	<b>3</b> <b>Proficient</b>	<b>2</b> <b>Nearly Proficient</b>	<b>1</b> <b>Developing</b>
<p>The student is able to:</p> <ul style="list-style-type: none"> <li>select and apply mathematical problem-solving techniques to discover complex patterns</li> <li>describe patterns as general rules consistent with correct findings</li> <li>prove, or verify and justify, these general rules.</li> </ul>	<p>The student is able to:</p> <ul style="list-style-type: none"> <li>Select and apply mathematical problem-solving techniques to correctly identify the pattern.</li> <li>Pattern is described as a relationship or general rule</li> <li>Verify the validity of these general rules.</li> <li>Conclusions are consistent with the correct findings.</li> </ul>	<p>The student is able to:</p> <ul style="list-style-type: none"> <li>Apply mathematical problem-solving techniques to recognize patterns.</li> <li>Suggest a relationship or general rule with findings.</li> </ul>	

*Analyzes proportional relationships and uses them to solve real-world and mathematical problems.*

: Computes unit rate associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units.

: Recognizes and represents proportional relationships between quantities.

: Uses proportional relationships to solve multi-step ratio and percent problems.

**ALT 4 - Proportional Relationships Rubric**

<p style="text-align: center;"><b>4</b> Highly Proficient</p>	<p style="text-align: center;"><b>3</b> Proficient</p>	<p style="text-align: center;"><b>2</b> Nearly Proficient</p>	<p style="text-align: center;"><b>1</b> Developing</p>
<ul style="list-style-type: none"> <li>• In addition to being proficient on the long-term target, I can demonstrate one or more of the following...</li> <li>• Consistently utilize efficient strategies to accurately solve problems in familiar situations</li> <li>• Apply understanding of long-term learning targets to unfamiliar situations and/or to solve complex problems</li> <li>• Use precise and relevant communication to justify mathematical thinking</li> <li>• Connect knowledge to other learning targets and/or advanced problem sets.</li> </ul>	<ul style="list-style-type: none"> <li>• Uses the concepts of ratio and ratio language to describe a ratio relationship between two quantities.</li> <li>• Uses the concept of a unit rate <math>a/b</math> associated with a ratio <math>a:b</math> with <math>b \neq 0</math>, and rate language in the context of a ratio relationship.</li> <li>• Uses ratios and rate reasoning to solve real-world and percent mathematical problems.</li> </ul>	<ul style="list-style-type: none"> <li>• I am beginning to and occasionally demonstrate proficiency of one or more of the following concepts...</li> </ul>	

*Applies and extends previous understandings of operations with fractions.*

: Applies and extends previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram.

: Applies and extends previous understandings of multiplication and division and of fractions to multiply and divide rational numbers.

: Solves real-world and mathematical problems involving the four operations with rational numbers.

**ALT 05 - Operations with Fractions Rubric**

<p style="text-align: center;"><b>4</b> Highly Proficient</p>	<p style="text-align: center;"><b>3</b> Proficient</p>	<p style="text-align: center;"><b>2</b> Nearly Proficient</p>	<p style="text-align: center;"><b>1</b> Developing</p>
<ul style="list-style-type: none"> <li>• In addition to being proficient on the long-term target, I can demonstrate one or more of the following...</li> <li>• Consistently utilize efficient strategies to accurately solve problems in familiar situations</li> <li>• Apply understanding of long-term learning targets to unfamiliar situations and/or to solve complex problems</li> <li>• Use precise and relevant communication to justify mathematical thinking</li> <li>• Connect knowledge to other learning targets and/or advanced problem sets.</li> </ul>	<ul style="list-style-type: none"> <li>• Applies and extends previous understandings of addition and subtraction to add and subtract rational numbers; represent addition and subtraction on a horizontal or vertical number line diagram.</li> <li>• Applies and extends previous understandings of multiplication and division and of fractions to multiply and divide rational numbers.</li> <li>• Solves real-world and mathematical problems involving the four operations with rational numbers.</li> </ul>	<ul style="list-style-type: none"> <li>• I am beginning to and occasionally demonstrate proficiency of one or more of the following concepts...</li> </ul>	

*Uses properties of operations to generate equivalent expressions, and solves real-world mathematical problems using numeric and algebraic expressions and equations.*

: Applies properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.

: Understands that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related.

: Solves multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form using tools strategically. Applies properties of operations; converts between forms as appropriate; and assesses the reasonableness of answers.

: Uses variables to represent quantities in a real-world or mathematical problems, and constructs simple equations and inequalities to solve problems by reasoning about the quantities.

**ALT 6 - Expressions and Equations Rubric**

<p style="text-align: center;"><b>4</b> Highly Proficient</p>	<p style="text-align: center;"><b>3</b> Proficient</p>	<p style="text-align: center;"><b>2</b> Nearly Proficient</p>	<p style="text-align: center;"><b>1</b> Developing</p>
<ul style="list-style-type: none"> <li>• In addition to being proficient on the long-term target, I can demonstrate one or more of the following...</li> <li>• Consistently utilize efficient strategies to accurately solve problems in familiar situations</li> <li>• Apply understanding of long-term learning targets to unfamiliar situations and/or to solve complex problems</li> <li>• Use precise and relevant communication to justify mathematical thinking</li> </ul>	<ul style="list-style-type: none"> <li>• Applies properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.</li> <li>• Understands that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related.</li> <li>• Solves multi-step real-life and mathematical problems posed with positive and negative rational numbers in any form using tools strategically.</li> <li>• Applies properties of operations; converts between forms as appropriate; and assesses the reasonableness of answers.</li> <li>• Uses variables to represent quantities in a real-world or</li> </ul>	<ul style="list-style-type: none"> <li>• I am beginning to and occasionally demonstrate proficiency of one or more of the following concepts...</li> </ul>	

<ul style="list-style-type: none"> <li>Connect knowledge to other learning targets and/or advanced problem sets.</li> </ul>	<p>mathematical problems, and constructs simple equations and inequalities to solve problems by reasoning about the quantities.</p>	
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*Draws, constructs, and describes geometric figures and relationships between them, and solves problems involving angle measure, area, surface area, and volume.*

: Solves problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale.

: Draws, with a variety of tools, geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.

: Describes the two-dimensional figures that result from slicing three-dimensional figures, as in plane sections of right rectangular prisms, and right rectangular pyramids.

: Knows the formulas for the area and circumference of a circle and uses them to solve problems; gives an informal derivation of the relationship between the circumference and the area of a circle.

: Uses facts about supplementary, complementary, vertical, and adjacent angles in a multi-step problem to write and solve simple equations for an unknown angle in a figure.

: Solves real-world and mathematical problems involving area, volume, and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms.

**ALT 7 - Geometric Figures and Measurement Rubric**

<p style="text-align: center;"><b>4</b> Highly Proficient</p>	<p style="text-align: center;"><b>3</b> Proficient</p>	<p style="text-align: center;"><b>2</b> Nearly Proficient</p>	<p style="text-align: center;"><b>1</b> Developing</p>
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<ul style="list-style-type: none"> <li>• In addition to being proficient on the long-term target, I can demonstrate one or more of the following...</li> <li>• Consistently utilize efficient strategies to accurately solve problems in familiar situations</li> <li>• Apply understanding of long-term learning targets to unfamiliar situations and/or to solve complex problems</li> <li>• Use precise and relevant communication to justify mathematical thinking</li> <li>• Connect knowledge to other learning targets and/or advanced problem sets.</li> </ul>	<ul style="list-style-type: none"> <li>• Solves problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale.</li> <li>• Draws, with a variety of tools, geometric shapes with given conditions. Focus on constructing triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.</li> <li>• Describes the two-dimensional figures that result from slicing three-dimensional figures, as in plane sections of right rectangular prisms, and right rectangular pyramids.</li> <li>• Knows the formulas for the area and circumference of a circle and uses them to solve problems; gives an informal derivation of the relationship between the circumference and the area of a circle.</li> <li>• Uses facts about supplementary, complementary, vertical, and adjacent angles in a multi-step problem to write and solve simple equations for an unknown angle in a figure.</li> <li>• Solves real-world and mathematical problems involving area, volume, and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms.</li> </ul>	<ul style="list-style-type: none"> <li>• I am beginning to and occasionally demonstrate proficiency of one or more of the following concepts...</li> </ul>
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*Develops understanding of statistical variability and investigates chance processes to develop, use, and evaluate probability models.*

: Understands that statistics can be used to gain information about a population by examining a random representative sample of a population.

: Uses data from a random sample to draw inferences about a population. Generate multiple samples (or simulated samples) of the same size to gauge the variation in estimates or predictions.

: Informally assesses visual overlap of two data distributions with similar variabilities, expressing the differences between centers as a multiple of a measure of variability.

: Uses measures of center and variability for numerical data from random samples to draw informal comparative inferences about two populations.

: Understands that the probability of a chance event is a number between 0 and 1 that expresses the likelihood of the event occurring.

: Approximates the probability of a chance event by collecting data, observing its long-run relative frequency, and predicting the approximate relative frequency.

: Develops a probability model and uses it to find probabilities of events. Compares probabilities from a model to observed frequencies; if the agreement is not good, explains possible sources of the discrepancy.

: Finds probabilities of compound events using organized lists, tables, tree diagrams, and simulations.

**ALT 8 - Statistics and Probability Rubric**

<p style="text-align: center;"><b>4</b></p> <p style="text-align: center;"><b>Highly Proficient</b></p>	<p style="text-align: center;"><b>3</b></p> <p style="text-align: center;"><b>Proficient</b></p>	<p style="text-align: center;"><b>2</b></p> <p style="text-align: center;"><b>Nearly Proficient</b></p>	<p style="text-align: center;"><b>1</b></p> <p style="text-align: center;"><b>Developing</b></p>
<ul style="list-style-type: none"> <li>• In addition to being proficient on the long-term target, I can demonstrate one or more of the following...</li> <li>• Consistently utilize efficient strategies to accurately solve problems in familiar situations</li> <li>• Apply understanding of long-term learning targets to unfamiliar</li> </ul>	<ul style="list-style-type: none"> <li>• Understands that statistics can be used to gain information about a population by examining a random representative sample of a population.</li> <li>• Uses data from a random sample to draw inferences about a population. Generate multiple samples (or simulated samples) of the same size to gauge the variation in estimates or predictions.</li> <li>• Informally assesses visual overlap of two data distributions</li> </ul>	<p>I am beginning to and occasionally demonstrate proficiency of one or more of the following concepts...</p>	

<p>situations and/or to solve complex problems</p> <ul style="list-style-type: none"> <li>• Use precise and relevant communication to justify mathematical thinking</li> <li>• Connect knowledge to other learning targets and/or advanced problem sets.</li> </ul>	<p>with similar variabilities, expressing the differences between centers as a multiple of a measure of variability.</p> <ul style="list-style-type: none"> <li>• Uses measures of center and variability for numerical data from random samples to draw informal comparative inferences about two populations.</li> <li>• Understands that the probability of a chance event is a number between 0 and 1 that expresses the likelihood of the event occurring.</li> <li>• Approximates the probability of a chance event by collecting data, observing its long-run relative frequency, and predicting the approximate relative frequency.</li> <li>• Develops a probability model and uses it to find probabilities of events. Compares probabilities from a model to observed frequencies; if the agreement is not good, explains possible sources of the discrepancy.</li> <li>• Finds probabilities of compound events using organized lists, tables, tree diagrams, and simulations.</li> </ul>	
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